# Self-Adaptive Generator Protection Methods

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## I. INTRODUCTION

The setting of many of the functions that are used to protect synchronous generators is relatively straightforward, requiring system or machine data that is readily available to the protection engineer. However, there are occasions where the effective application of a protection function requires detailed measurement and analysis of operational data from the machine. This paper identifies two such functions: Split Phase protection and 3<sup>rd</sup> Harmonic Neutral Undervoltage protection and discusses the particular application issues associated with each. These functions are responsible for detection of two of the most common types of stator winding failures; inter-turn faults and ground faults. A new algorithm is presented that can respond to the influencing system conditions and automatically adapt these functions accordingly. The resulting protection schemes are more sensitive, less likely to mis-operate, and are easier to set than their conventional counterparts.

# II. INTERTURN FAULTS

A hydroelectric generator is often wound with a double-layer, multi-turn winding. The winding may be a single circuit or there may be two, four, six or eight branches in parallel. Under normal operation there is very little difference in the current in each branch. However, during an internal fault, currents will circulate between the parallel branches of the winding within one phase. Split phase protection takes advantage of this characteristic by measuring the current unbalance between these parallel branches. In hydro machines a significant percentage of stator faults begin as turn-to-turn faults [1]. Due to the very high effective turns-ratio between the windings and the shorted turn, inter-turn

faults cause extremely high currents in the faulted loop leading to quickly progressing damage.

These faults are not detectable by the stator differential or ground fault protections since there is no difference between the currents at the output and the neutral terminals and there is no path for fault current to ground. If these faults can be detected before they evolve in to phase or ground faults then the damage to the machine and associated downtime can be greatly reduced. Therefore the split phase protection should ideally be sensitive enough to operate for a single-turn fault in the winding of the machine.

## A. Detection Methods

There are several methods currently in use today.

## 1) Scheme A

In scheme A, a neutral point is brought out for each parallel circuit. An overcurrent element is connected between each neutral. During an inter-turn fault, a circulating current is produced in the faulted phase that is passed between the neutrals.

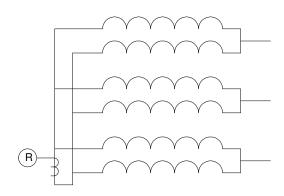


Figure 1 - Scheme A

## 2) Scheme B

In this scheme a differential and restraint signal are derived using currents from both sides of the machine. One current represents the total current in the machine while the other is the current from a CT representing 1/2 the total current. This scheme is also known as "combined split phase and differential" or "partial longitudinal differential".

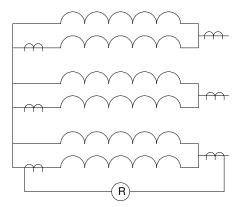


Figure 2 - Scheme B

#### 3) Scheme C

In scheme C, the currents from each parallel circuit are used to derive a differential and restraint signal. The relay has a percent slope characteristic. The restraint signal provides security against a false differential produced during an external fault while still allowing fast operation during internal faults. This scheme is sometimes known as "transverse differential".

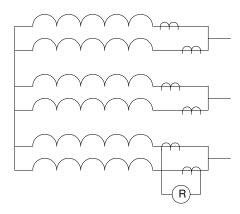


Figure 3 - Scheme C

## 4) Scheme D

The scheme shown in Figure 4 also responds to the difference between the currents in the two circuits. However, the summation is done outside the relay.

Therefore this method cannot derive a restraint signal. An instantaneous element using this signal must be set high enough to avoid pickup during an external fault. This will make the element relatively ineffective for detection of single-turn faults. As such this scheme usually employs a definite time or inverse time characteristic for security.

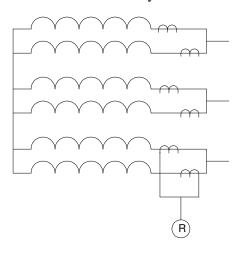


Figure 4 - Scheme D

# 5) Scheme E

In this scheme a window-type CT is used to measure the difference between the current in each circuit, as shown in Figure 5. This method avoids the CT error issues of Scheme D.

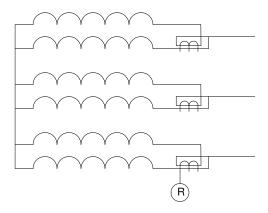


Figure 5 - Scheme E

## B. Characterization

Under normal operation the level of the inherent split phase current is usually less then 0.5% of the rated machine current [1]. During an external fault many machines produce a transient circulating current. The magnitude of this transient can be several times larger than the steady state current and may persist for upwards

of 30 cycles [1]. For an internal fault, the magnitude of the circulating current corresponding to a single-turn short is dependent on several factors. These include the type of the winding (adjacent versus alternate pole) and the number of poles.

## C. Application

A simple calculation can be carried out to approximate the circulating current due to a shorted turn as shown in the example system of Figure 6.

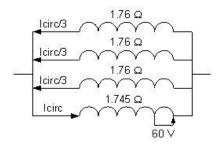


Figure 6 Interturn Fault

The machine in this example is rated at 65MVA and 13.8 kV. The stator winding has 4 parallel circuits, each made of 33 series coils and each coil having 4 turns. The rated current is 2700 amps. The winding impedance can be approximated by the leakage reactance (0.15 p.u in this case). Each healthy parallel branch will have 4 times the nominal impedance or 1.76 ohms. The impedance of a single turn is 0.013 ohms. The voltage across a single turn is 60 volts.

$$V_{\text{turn}} = \frac{V_{\text{nominal}}}{\sqrt{3} \cdot N_{\text{turns}} \cdot N_{\text{coils}}} = 60$$

$$I_{circ} = \frac{V_{turn}}{Z_{circuit} - Z_{turn} + \frac{Z_{circuit}}{N_{circuit} - 1}} = 26$$

This corresponds to a circulating current of about 1% of rated current.

## D. Bypassed Coil

A failure in the winding of a machine requires its immediate removal from service until repairs have been carried out. Often the machine may be supplying critical load to the system. In this instance it is possible to carry out temporary repairs to the machine and place it back in service. These repairs typically entail isolating and bypassing the faulty coil. A machine operated under these conditions may be subject to overheating,

magnetic pullover and excessive vibration requiring that it be operated at a reduced load level. In the context of this paper, the bypassed coil can potentially have a dramatic impact on the inherent split phase current [2].

Figure 7 shows one phase of a machine with M parallel branches and a bypassed coil in one branch. The quantity  $X_{CC}$  can be approximated by the leakage reactance  $X_L$  [3].

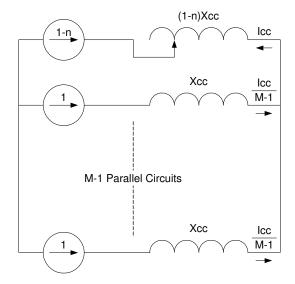


Figure 7 - Operation with a Bypassed Coil

The quantity n represents the number of coils bypassed expressed in per-unit. Inspection of the circuit illustrates the effect of a bypassed coil on the circulating current. It is evident that an interturn fault in a healthy branch (without a bypassed coil), can act to bring the circulating current back towards equilibrium; i.e. the fault may not necessarily translate into an increase in the split-phase current magnitude.

Figure 8 shows the split phase current in a model machine with a small portion of the stator winding bypassed in one phase. Power is displayed in per unit and split phase current in secondary amps. The bypassed winding creates a significant increase in the inherent split phase current. Additionally, the magnitude of the split phase current displays a strong dependency on real and reactive power.

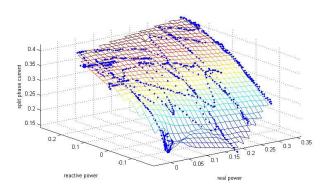


Figure 8 - Split Phase Current Measurements

As a result the pickup setting of the split phase protection must be increased to prevent false operation. This can make the function ineffective for the detection of single-turn faults.

#### III. STATOR GROUND FAULTS

Stator ground faults are short circuits between any of the stator windings and ground, via the iron core of the stator. Typically, when a single machine is connected to the power system through a step-up transformer, it is grounded through high impedance. As a result, the amount of the short circuit current during stator ground faults is driven by the amount of capacitive coupling in the machine and its step-up transformer. Therefore when a ground fault occurs, very small capacitive current flows making the short circuit difficult to detect.

Ground faults can be detected throughout most of the winding through the use of an overvoltage relay responding to the fundamental component of the voltage across the grounding impedance. The magnitude of this voltage is proportional to the location of the fault. Therefore, for faults at or near the neutral of the machine, this element is ineffective [4].

Little or no damage is done to the machine as a result of a ground fault close to the neutral. It does, however, prevent the overvoltage protection from detecting a second ground fault. If a second ground fault occurs, the grounding impedance does not limit the fault current. If the second ground is on the same phase it will not be detectable by the differential. The result can be potentially catastrophic damage to the machine [5]. Therefore, a second method to detect faults close to the neutral and effectively prevent widespread damage to the machine is beneficial. This second method is sometimes known as 100% stator ground fault protection.

# A. Methods for Detection

Several techniques for 100% stator ground fault detection take advantage of the third harmonic voltage generated by the machine itself [5].

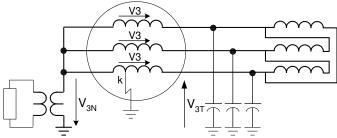
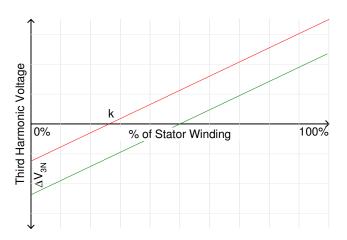


Figure 9 Stator Ground Fault

Under normal operating conditions a portion of the 3<sup>rd</sup> harmonic appears across the generator terminals and a portion appears across the grounding impedance as shown by the green line in Figure 10. For a fault at k, the distribution of the third shifts to the red line. This causes the third harmonic at the neutral to decrease and the third harmonic at the terminals to increase.



**Figure 10 Third Harmonic Distribution** 

If the third harmonic can be measured both at the generator neutral and at the terminals, then a differential scheme can be applied [5]. This scheme is less sensitive to variations in the third harmonic due to machine loading. However, if the VT connection does not permit measurement of the third harmonic at the generator terminal end [5], comparison of the neutral and terminal end third harmonic signatures is impossible, and then only the third harmonic neutral undervoltage element may be applied.

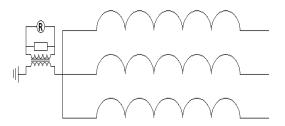


Figure 11 - Neutral Undervoltage Scheme

The third harmonic undervoltage element uses the voltage that forms across the high impedance ground, which is connected to the neutral point of the generator unless a better path to ground is presented. Figure 12 is an example of the third harmonic voltage measured at the neutral of a generator at various levels of real and reactive loading. Power is displayed in primary units and third harmonic voltage is displayed in secondary volts. During a ground fault close to the generator neutral the third harmonic voltage will decrease or drop to zero.

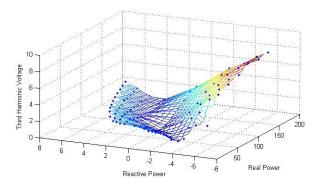


Figure 12 - Third Harmonic Voltage Characteristic

In the scheme of Figure 11 a neutral voltage is measured from the machine neutral point. During a stator ground fault, the third harmonic will flow into the ground fault, shunting the neutral grounding path, and the measurement of neutral voltage will drop to or near zero.

## B. Characterization

The characteristic of the third harmonic varies considerably between different machine designs; it can also vary considerably between machines of the same design due to manufacturing variation. Under normal operation the level of the third harmonic neutral voltage can vary considerably based upon machine output (MW), power factor (PF) and machine voltage (kV).

In order to provide optimum protection for the machine, the complete third harmonic characteristic must be found and the setting should be calculated based on this data. Data must be collected and then plotted with output (MW) along the X-axis and third harmonic neutral voltage (V) along the Y-axis as shown in Figure 13.

Once this data is plotted an appropriate tripping voltage should be determined. It should be significantly high such that the protection will function, even when the fault is farther up on the winding. The setting must also allow enough margin to allow for variation and errors in the data collection and input accuracy.

A power blocking value should be derived so that it complements the tripping voltage. The local minimums in the third harmonic characteristic should be blocked allowing the highest possible tripping voltage.

There are several options for setting this function.

## 1) Type Testing

A simple method of setting this function utilizes the data from type tests for machines of the same design. Electrical machines of the same design and manufacture can be type tested and a standard set point can be calculated and used. This provides the easiest solution however it is the least effective and can provide less protection or lead to nuisance tripping.

# 2) Site Testing

The setting can be derived by taking site data for each machine by running the machine through the range of power output and power factor. Taking data at regular intervals will allow for a sufficiently accurate setting to allow for protection while keeping from false tripping. This method is provides good protection but is more expensive than type tests and still allows the opportunity for data collection errors. An example of the data collected during a site test is shown in Figure 13.

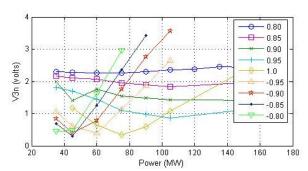


Figure 13 – Third Harmonic Neutral Voltage Data

## C. Electronic Data Collection

If a data logger with sufficient memory exists in the applied protective relay [7], data logging can be used to collect operating data over the operating time. This data can be extracted from the data logger and used to calculate the setting. This method provides much more accurate characterization of the third harmonic, however the data may not cover the entire operating region. If the machine has not operated in those regions the protection setting decision may be made with incomplete data, which could lead to nuisance tripping or insufficient protection.

## IV. SELF-ADAPTIVE PROTECTION PRINCIPLES

The previous sections describe the deviation that can sometimes occur in the operating signals of the split phase and 3<sup>rd</sup> harmonic undervoltage element as a result of active and reactive loading of the machine and the resulting problems relating to setting selection. It is proposed that for both functions a method could be derived to automatically adapt to these variables.

The method would measure and log the variations in the operating quantity over time in order to learn the characteristics under various loading conditions and operate based on a departure from this characteristic in order to protect the machine.

Implemented in a microprocessor-based device, data collection would entail sampling the voltages and currents and the operating quantities, filtering digitally, extracting magnitudes/angles using a standard Fourier algorithm, and calculating active and reactive quantities from these.

The method would allow for the protection to become active as soon as the data has been collected. The function could be proactively enabled and disabled to protect for operating conditions where sufficient

operation data has been collected and block for operating conditions where insufficient data has been collected.

The function would require a security margin to account for measurement errors.

A best-fit curve could be calculated to approximate the operating characteristic; there are several methods for forming this function. This method would require recalculation of the curve each time data is collected and would be very processor intensive.

Alternately, the operating characteristic could be approximated by an array of data points stored to create a mesh of operating signal values spaced equally over the active-reactive power region. This method requires more memory to store the data but is less processorintensive.

Data would be collected whenever the machine is in operation. The data would be used to update the array holding the operating data for the machine. Since the array consists of a finite number of elements, the measured value of the operating signal data would not usually correspond exactly to a point in the array (points I-IV in Figure 14).

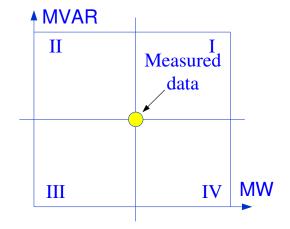


Figure 14 - Operating Data Array

Therefore either the point closest to the measured value could be updated or all four adjacent points could be updated simultaneously.

Before the data could be used for fault detection the data must be validated. This could be a manual operation – the data could be downloaded and analyzed. If satisfactory the function could then be placed in-service.

Alternately, the validation of the data could be automated. In such a scheme, a test could be carried out on the data to determine whether or not it is changing dramatically between successive samples. An additional test would be to examine the smoothness of the characteristic over successive data points.

An important consideration is the number of points in the array required for an accurate representation of the data. The factors influencing this determination include the smoothness of the operating characteristic, the method used to interpolate between points in the array and the accuracy required by the function.

Once the data has been validated it may be used for fault detection. Again, it is unlikely that the measured value of P and Q will correspond to a point in the array.

An expected operating value must therefore be calculated for each value of P and Q. Since this function is adaptive the value must be calculated in real time.

Terminal voltage can have a significant effect on the quiescent value of the operating signal. The signal can be similarly affected during other system disturbances. Therefore it is important to inhibit learning during these periods. This can be achieved by monitoring of the positive sequence voltage and current. Learning is inhibited if the positive sequence voltage is lower than its nominal range. Learning is also inhibited when the positive sequence current is greater than its nominal value. Additionally, some machines may exhibit a significant difference in the operating signal between the offline and online state. In such cases, learning may also be supervised by breaker position. Once system conditions return to normal for a definite period, normal learning can resume. Similar supervision can be applied in the tripping mode.

## V. DEVELOPMENT OF ADAPTIVE ALGORITHMS

As explained in the previous section adaptive algorithms in this application consist of two parts. First, a learning procedure is required to establish the operate/restraint surface based on the measured data over longer periods of time. Second, an operate logic is required to use the learned surface for tripping at a given time.

This section presents practical ways of implementing such algorithm. The equations are derived for twodimensional situations, i.e. when a single operating quantity depends on two variables, but can be easily extended onto generalized multi-dimensional cases.

## A. Learning Procedure

With reference to Figure 15, an operating quantity X under non-fault conditions in a function of two variables, P and Q. In our application P and Q are active and reactive power in the export direction, and X is the window CT current magnitude or angle in case of splitphase protection, and the third harmonic voltage magnitude in the case of stator ground fault protection.

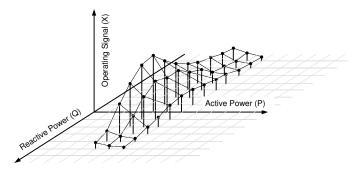


Figure 15 - Normal Operation Surface

The normal operation surface is represented by a finite amount of points in the form of a grid. Assuming the same grid size for the active and reactive power,  $\Delta$ , the grid coordinates are:

$$P_i = \Delta \cdot i, \quad i = 0 \dots N_{\text{max}} \tag{1a}$$

$$Q_j = \Delta \cdot j, \quad j = -M_{\text{max}} \dots M_{\text{max}}$$
 (1b)

Note that the active power is assumed positive, as there is no need to keep this method operational under the short periods of abnormal reverse-power operation of the machine. If needed, the implementation can easily be extended to cover all four quadrants of power.

During normal or abnormal operation of the machine, the measuring unit of the relay, returns the following operating point:

$$(X, P, Q) \tag{2}$$

First, this point must be related to the finite grid representing the operate/restraint surface:

$$p = floor\left(\frac{P}{\Delta}\right) \tag{3a}$$

$$q = floor\left(\frac{Q}{\Delta}\right) \tag{3b}$$

Where floor stands for rounding down to the nearest integer.

The operating point is located between the following four corners of the grid (Figure 16):

$$(p,q), (p,q+1), (p+1,q+1), (p+1,q)$$
 (4)

During the learning phase, the value of X shall be used to adjust all four corners surrounding the operating point. Different approaches can be used.

In one method, all four points are treated equally and use the same value to adjust the value of the learned X. For example:

$$X_{(p,q)NEW} = (1 - \alpha) \cdot X_{(p,q)OLD} + \alpha \cdot X$$
 (5a)

In the above, a smoothing filter is used for extra security. Only a small fraction of the measurement ( $\alpha$ ) is added to the previous value. In this way the sought value at the (p, q) point of the grid reaches its steady state asymptotically, and the value of  $\alpha$  controls the speed of learning. The higher the  $\alpha$ , the faster will be the convergence.

Similar equations are used to adjust the other three corners around the measuring point:

$$X_{(p,q+1)NEW} = (1-\alpha) \cdot X_{(p,q+1)OLD} + \alpha \cdot X \tag{5b}$$

$$X_{(p+1,q+1)NEW} = (1-\alpha) \cdot X_{(p+1,q+1)OLD} + \alpha \cdot X$$
 (5c)

$$X_{(n+1,\alpha)NEW} = (1-\alpha) \cdot X_{(n+1,\alpha)OLD} + \alpha \cdot X \tag{5d}$$

In another method, the closer the operating point to a given point of the grid, the higher the impact on the learned value for that point of the grid. This can be accomplished using the following equations for learning.

First, the relative distances between the operating point and the four corners are calculated:

$$D_{(p,q)} = \frac{\left(p \cdot \Delta - P\right)^2 + \left(q \cdot \Delta - Q\right)^2}{2 \cdot \Lambda^2} \tag{6a}$$

$$D_{(p,q+1)} = \frac{(p \cdot \Delta - P)^2 + (q \cdot \Delta + \Delta - Q)^2}{2 \cdot \Delta^2}$$
 (6b)

$$D_{(p+1,q+1)} = \frac{(p \cdot \Delta + \Delta - P)^2 + (q \cdot \Delta + \Delta - Q)^2}{2 \cdot \Delta^2}$$
 (6c)

$$D_{(p+1,q)} = \frac{(p \cdot \Delta + \Delta - P)^2 + (q \cdot \Delta - Q)^2}{2 \cdot \Delta^2}$$
 (6d)

These distances can be used to speed up the learning for corners located closer to the operating point:

$$X_{(p,q)NEW} = \left(1 - \alpha \cdot \left(1 - D_{(p,q)}\right)\right) \cdot X_{(p,q)OLD} + \alpha \cdot \left(1 - D_{(p,q)}\right) \cdot X$$

$$(7a)$$

$$\begin{split} X_{(p,q+1)NEW} = & \left(1 - \alpha \cdot \left(1 - D_{(p,q+1)}\right)\right) \cdot X_{(p,q+1)OLD} \\ & + \alpha \cdot \left(1 - D_{(p,q+1)}\right) \cdot X \end{split} \tag{7b}$$

$$\begin{split} X_{(p+1,q+1)NEW} = & \left(1 - \alpha \cdot \left(1 - D_{(p+1,q+1)}\right)\right) \cdot X_{(p+1,q+1)OLD} \\ & + \alpha \cdot \left(1 - D_{(p+1,q+1)}\right) \cdot X \end{split}$$

$$\begin{split} \boldsymbol{X}_{(p+1,q)NEW} = & \left(1 - \alpha \cdot \left(1 - D_{(p+1,q)}\right)\right) \cdot \boldsymbol{X}_{(p+1,q)OLD} \\ & + \alpha \cdot \left(1 - D_{(p+1,q)}\right) \cdot \boldsymbol{X} \end{split} \tag{7d}$$

Version (7) has an advantage over version (5) when the operating point lingers at the border line between two different segments of the grid – it provides smooth transition between training one set of point versus a different set of points on the grid.

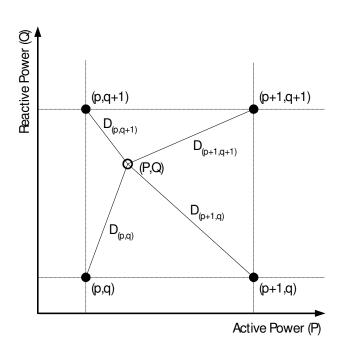


Figure 16 - Calculation of Distances

Equations (5) and (7) average the data when forming the operate/restraint surface by means of exponential convergence. A separate check must be designed to decide if a given value learned in the process is final and could be trusted, i.e. used by the operating logic.

Two criteria are used to decide if a given point is properly trained.

First, it is checked if the update process as dictated by equation (5) or (7) stops changing the value. This is determined by checking the increment after the update takes place. For example, when using form (7) one checks:

$$FLG_{1(p,q)} = \left| X_{(p,q)NEW} - X_{(p,q)OLD} \right| < \beta \cdot X_{(p,q)NEW}$$
 (8)

Where  $\beta$  is an arbitrary value expressing the percentage difference that identifies the steady state is being reached.

The above flag is calculated each time a given point on the grid is updated as a part of the learning procedure that is for all four points surrounding the operating point.

Second, it is checked with the surface emerging in response to learning is smooth. This is determined by checking differences between the surrounding points on the grid:

$$\begin{split} FLG_{2(p,q)} &= \left| X_{(p,q)} - X_{(p-1,q)} \right| < \delta \cdot X_{(p,q)} \ \& \qquad \dots \\ &\dots \& \left| X_{(p,q)} - X_{(p+1,q)} \right| < \delta \cdot X_{(p,q)} \ \& \qquad \dots \\ &\dots \& \left| X_{(p,q)} - X_{(p,q-1)} \right| < \delta \cdot X_{(p,q)} \ \& \qquad \dots \\ &\dots \& \left| X_{(p,q)} - X_{(p,q+1)} \right| < \delta \cdot X_{(p,q)} \ \& \qquad \dots \end{split}$$

Where  $\delta$  is an arbitrary factor. Equation (9) takes exception for the points on the outer border of the grid – these points have only three, not four, neighboring points.

For a given point on the grid (p, q) to be considered trained, both the flags (8) and (9) must be asserted.

The learning procedure can be summarized as follows:

- 1. Take the measurement of the operating point (equation (2)).
- 2. Calculate the coordinates of the grid (equation (3)).
- 3. Update the four corners of the grid surrounding the operating point (equations (6) and (7)).
- 4. Calculate the first validity flag for the four updated points (equation (8)).
- 5. Calculate the second validity flag for the four updated points and their neighbors (equation (9)).
- 6. Update the validity flags for the affected points on the grid.

## VI. SIMULATION RESULTS

Figures 17-21, illustrate the learning procedure using an arbitrary surface. In this example the operating quantity is given by the following equation:

$$X = P \cdot e^{P^2 + Q^2} \tag{10}$$

For the third harmonic undervoltage function the following design constants are selected:

$$\Delta = 0.05 \, pu$$
,  $N_{\text{max}} = 25$ ,  $M_{\text{max}} = 25$ 

$$\alpha = 0.05$$
,  $\beta = 0.03$ ,  $\delta = 0.03$ .

For the split phase function the following design constants are selected for both the current magnitude and angle:

$$\Delta = 0.125 \, pu, \quad N_{\text{max}} = 10, \quad M_{\text{max}} = 10$$
 $\alpha = 0.05, \quad \beta = 0.03, \quad \delta = 0.03.$ 

The above means the (P, Q) grid stretches as follows (0,1.25pu) for the active, and the reactive power.

Figure 17 presents function (10). This is the target function that should be learned by the procedure.

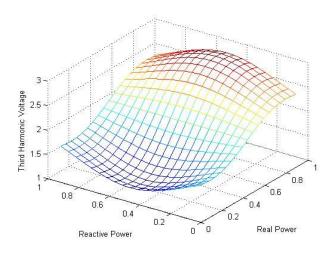


Figure 17 - Simulated 3rd Harmonic Characteristic

During the training, the operating point was varied randomly to wander within the assumed (P, Q) space. For each (P, Q) pair, the X value was calculated per equation (10), thus creating the measured operating point per equation (2). This operating point was injected into the learning algorithm.

Figures 18,19 & 20 present the shape of the operate/restraint surface at various stages of the

learning.

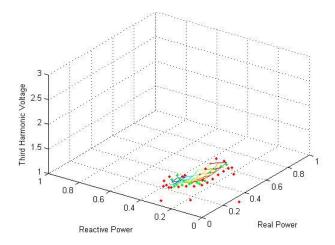


Figure 18 - Learned Data at 1.7 hr at 1 sample/sec

These plots display the validity flags for the points on the grid – red dotes stand for "not learned", and green dots signify "learned" points of the surface.

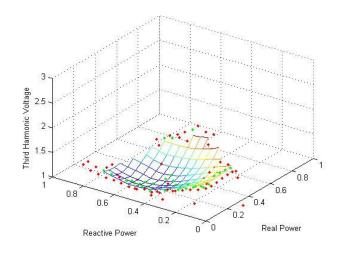


Figure 19 - Learned Data at 3.4 hr at 1 sample/sec

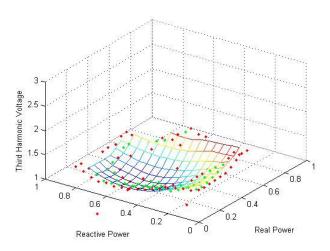


Figure 20 - Learned Data at 5 hr at 1 sample/sec

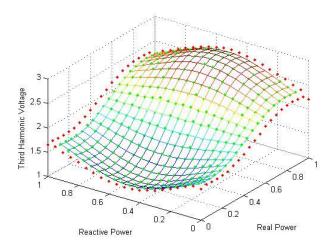


Figure 21 - Final Learned Data

Figure 21 shows the final learned surface at the end of the process. This shape is identical with the assumed model of the process (10), proving the learning procedure is stable and capable of re-creating the process.

## VII. TRIPPING LOGIC

Before the learned surface can be used to detect sudden changes and be used for tripping, the validity of the learned points on the (P, Q) grid needs to be verified. With reference to Figure 16, a given measurement point is approximated by four surrounding corners on the grid. Operation (3) is executed as a part of the tripping logic to obtain the grid coordinates. All four corners (p, q), (p, q+1), (p+1,q+1), (p+1,q) must be valid in order to proceed.

When valid, the four corners are used to interpolate the expected value of the operating signal. A weighted average can be used for this approximation:

$$D = D_{(p,q)} + D_{(p,q+1)} + D_{(p+1,q+1)} + D_{(p+1,q)}$$
 (11a)

$$X_{EXPECTED} = \frac{1}{D} (X_{(p,q)} \cdot D_{(p,q)} + X_{(p,q+1)} \cdot D_{(p,q+1)} + \dots$$

...+ 
$$X_{(p+1,q+1)} \cdot D_{(p+1,q+1)} + X_{(p+1,q)} \cdot D_{(p+1,q)}$$
 (11b)

Where the four distances are calculated for a given value of X using equations (6).

The tripping logic checks for differences between the expected and actual values.

The third harmonic undervoltage function operates if:

$$V_{3N} < X_{EXPECTED} - \Omega \tag{12}$$

Where  $\Omega$  is a security margin.

The split-phase protection operates if

$$|I_{SP} - |X1_{EXPECTED}| \angle X2_{EXPECTED}| > \Pi$$
 (13)

Where  $\Pi$  is a security margin. The characteristic for the split phase function is illustrated in Figure 22

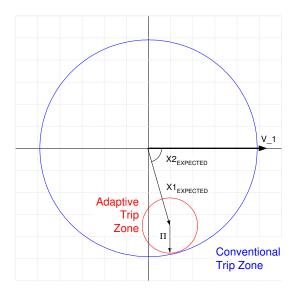


Figure 22 Adaptive Split Phase Function

In the above operating equations the security margins can be expressed as a fixed values, or as percentages of the expected value, or both in a combination.

Separate learning procedures are executed for the third harmonic undervoltage function, and for each phase of the split phase overcurrent function.

In a practical device it will be necessary to export and import learned data if, for instance the protective device is replaced. Also it will be necessary to signal to the algorithm that a repair has been carried out and it is necessary to re-evaluate the learned data

#### VIII. CONCLUSIONS

In the area of generator protection the current state of microprocessor-based technology presents opportunities to overcome the limitations of conventional protection schemes. This paper has focused on two candidates: split phase protection and third harmonic undervoltage. It has been shown that these functions can present challenges for effective application. It has also been demonstrated that adaptive algorithms can be designed to circumvent these problems and can result in a function that is more sensitive over a wider range of operation.

Moving forward the authors intend to prototype the algorithms in a microprocessor-based device and carry out field trials on in-service machines in order to validate the methods, optimize the design constants used in the algorithm, and identify possible opportunities for improvement.

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## **BIOGRAPHIES**

Dale Finney received his Bachelor of Engineering degree from Lakehead University in 1988. He began his career with Ontario Hydro where he worked as a protection and control engineer. Currently, Mr. Finney is employed as an Applications Engineer with GE Multilin. His areas of interest include generator protection, distance protection, and substation automation. Mr. Finney is a registered professional engineer in the province of Ontario and is a member of the IEEE and PSRC.

**Bogdan Kasztenny** holds the position of Protection and System Engineering Manager for the protective relaying business of General Electric. Prior to joining GE in 1999, Dr.Kasztenny conducted research and taught protection and control at Wroclaw University of Technology, Texas A&M University, and Southern Illinois University.

Between 2000 and 2004 Bogdan was heavily involved in the development of the Universal Relay<sup>TM</sup> series of protective IEDs, including a generator protection relay.

Bogdan authored more than 140 papers, is the inventor of several patents, a Senior Member of the IEEE, and serves on the Main Committee of the PSRC.

In 1997, he was awarded a prestigious Senior Fulbright Fellowship. In 2004 Bogdan received GE's Thomas Edison Award for innovation.

**Gustavo Brunello** received his Engineering Degree from the National University in Argentina and a Master in Engineering from University of Toronto. He also attended a 2 year post-graduate course in Power Systems Engineering at Polytechnic of Turin (Italy).

After graduation he worked for the National Electrical Power Board in Argentina where he was involved in testing and commissioning the 500 kV backbone transmission system. He then joined NEI Reyrolle (England) were he specialized in protective relays. For several years he worked with ABB Relays and Network Control both in Canada and Italy. In 1999, he joined GE Power Management (Multilin) as a Senior Application Engineer. Presently, he is Regional Sales Manager

André Lacroix is a professional engineer. He graduated from Polytechnique of Montréal in 1983 and began his career as a consultant in the design of electrical substations including protection and control. He has also been employed with a start-up & commissioning services firm concerned with protection for cogeneration projects in northern Ontario and consulting for Hydro Québec projects. Since 1992 he has been employed with Hydro Québec in the roles of control engineer, project engineer, and generator protection engineer.

Michael McClure received his Bachelors degree from Clarkson University in 2003. He began his career as an Edison Engineering Development Program member and has worked as a generator design engineer and generator protection system engineer. Currently, Mr. McClure is employed as a generator protection engineer with GE Energy. His areas of interest include Generator Protection and Excitation.